# Supplemental Material: Gait Cycle Validation and Segmentation using Inertial Sensors 

G.V. Prateek, Pietro Mazzoni, Gammon M. Earhart, and Arye Nehorai

Appendix A

```
Algorithm 2 Gait Cycle Validation and Segmentation Algorithm
    procedure \(\operatorname{GCVS}\left(\boldsymbol{A}, \boldsymbol{C}, \lambda, \mu, \gamma_{\mathrm{D}}, \gamma_{\mathrm{GCVS}}, \sigma_{a}^{2}, \sigma_{\omega}^{2}\right)\)
        \(k \leftarrow 0, i \leftarrow 0\)
\(\mathrm{MS} \leftarrow\}, \mathrm{TO} \leftarrow\{ \}, \mathrm{HS} \leftarrow\{ \}\)
        loop
            \(k \leftarrow k+1 \quad \triangleright\) Increment sample counter
            Compute \(T_{k}\left(\boldsymbol{y}^{\mathrm{a}}, \boldsymbol{y}^{\omega}\right)\)
            if \(T_{k}\left(\boldsymbol{y}^{\mathrm{a}}, \boldsymbol{y}^{\boldsymbol{\omega}}\right)<\gamma_{\mathrm{D}}\) then
                    if \(\boldsymbol{y}^{\omega_{\mathrm{s}}}\) is not empty then
            Scale and interpolate \(\boldsymbol{y}^{\omega_{\mathrm{s}}}\)
            Extract DWT coefficients \(\boldsymbol{k}_{i}\) using SAWD algorithm
            Compute \(\mathrm{RMSE}_{i}\) using \(\boldsymbol{k}_{i}\) and \(\boldsymbol{k}_{\mathrm{T}}\)
            if \(\mathrm{RMSE}_{i}<\gamma_{\text {GCVS }}\) then
                        \(i \leftarrow i+1\)
                            Determine \(\mathrm{TO}_{i}\), and \(\mathrm{HS}_{i}\)
                        Reset \(\boldsymbol{y}^{\omega_{\mathrm{s}}}\)
                    end if
                    end if
                    Store \(T_{k}\left(\boldsymbol{y}^{\mathrm{a}}, \boldsymbol{y}^{\omega}\right)\) in \(\boldsymbol{z}^{\mathrm{a}, \omega} \quad \triangleright\) To find midstance event
            else
                    if \(z^{\mathrm{a}, \omega}\) is not empty and \(M_{i}>0.1\) seconds then
                            Determine \(\mathrm{MS}_{i}\)
                    end if
                    Reset \(\boldsymbol{z}^{\mathrm{a}, \omega} \quad \triangleright\) An empty vector
                    Store \(\left[\boldsymbol{y}^{\omega}\right]_{k}\) in \(\boldsymbol{y}^{\omega_{\mathrm{s}}} \quad \triangleright\) To find toe-off and heel-strike events
            end if
        end loop
        return MS, TO, HS
    end procedure
```


## Appendix B

In the treadmill experiment, as a reference system, we used a GoPro camera placed a few feet away from the treadmill (see Fig. 1). In addition, a digital clock was also placed next to the treadmill, so that the readings on the clock were clearly captured in the video data. The digital clock readings were used to manually synchronize the video data with the inertial sensor data. We used the following definition of a valid gait cycle to determine the ground truth:
"A gait cycle in the video data is defined as a valid gait cycle if it contains exactly one heel-strike and one toe-off event, in that order, between two consecutive midstance events."


Fig. 1: Snapshot of the video data collected in the treadmill experiment to determine the ground truth.

## Appendix C



Fig. 2: Daubechies ( db 4 or D 8 ) wavelet function.

## Appendix D

TABLE 1: Summary of the datasets validated in this work.

| Table \# | Sensor Type | Sampling Rate | Sensor <br> Location | \# of Participants |  |  | Healthy | PD |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $F_{\mathrm{s}}$ | Geriatric | \# of Strides <br> Training Data | Total \# of Strides |  |  |  |

Remarks: When the sensor is attached to the instep region of the foot, with the help of FSR and inertial sensors, it was verified in [12], [13] that the local minima of the gyroscope signal in the sagittal plane represent the toe-off and heel-strike events. For the instep region, we validate the ON-GCVS in Table II and III. In Table II, we compute the number of valid gait cycles detected, and also the gait parameters, i.e., toe-off angle, heel-strike angle, and swing as $\%$ of gait cycle, and compare our implementation of the inertial navigation system with the results obtained using a proprietary software, MLBS (Mobility Labs Software). The MLBS software uses the algorithm proposed by Salarian et al. to detect gait events, such as heel-strike and toe-off events. In Table III, we validate the number of gait events detected by the proposed ON-GCVS method and the existing MLBS method.

For the datasets in Table IV and V, i.e., when the sensor is attached to the heel region (in the sagittal plane), we only validate the number of gait cycles. We cannot validate the gait parameters observed at gait events, such as heel-strike and toe-off events because the ground truth information for these parameters is not available in database [16]. The database only consists of time instances of valid gait cycles and not the gait parameters observed during these valid gait cycles. Furthermore, the datasets used in Table III and IV are also not compatible with the Mobility Labs Software (MLBS) because the MLBS is a proprietary software that works only when the inertial sensor data is collected using the APDM Opal sensor.

Similarly, for the datasets in Table VI, i.e., when the sensor is attached to the heel region (in the frontal plane), we only validate the number of gait cycles. The ground truth in this case was obtained using video data, which captures the validity of a gait cycle and does not determine the gait parameters observed at these valid gait cycles. Furthermore, the datasets used in Table VI are also not compatible with the Mobility Labs Software (MLBS).

Our main contribution in this work is the gait cycle validation algorithm presented in Section III, i.e., given any nonstationary segment of the gyroscope measurement in the sagittal plane, our proposed method determines if it is a valid gait cycle or not. The validation of the gait parameters observed at gait events, such as heel-strike and toe-off, depends on the implementation of the inertial navigation system (INS). An INS can be implemented in many different ways depending on the sensors and the pseudo measurements used to correct the states of the Kalman filter. In our work, we used the sensor measurements from the accelerometer and gyroscope, and zero-velocity event intervals as pseudo measurements, to estimate the position, velocity, and orientation estimates of the foot. In Table II, we validated the implementation of our INS by computing gait parameters observed at gait events, such as toe-off and heel-strike events, and compare our implementation of the INS with the results obtained using the MLBS.

## Appendix E

TABLE 2: Performance of the existing and proposed methods for the 12 meter walk task.

| Method | Dataset | Free WALK |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $F_{\text {s }}=125 \mathrm{~Hz}$ |  |  |  | $F_{\text {s }}=250 \mathrm{~Hz}$ |  |  |  | $F_{\mathrm{s}}=500 \mathrm{~Hz}$ |  |  |  |
|  |  | Precision | Recall | F1-Score | Time | Precision | Recall | F1-Score | Time | Precision | Recall | F1-Score | Time |
| OFF-PDT | TT003 | 91.66\% | 100.0\% | 95.65\% | 0.101 | 91.66\% | 100.0\% | 95.65\% | 0.103 | 91.66\% | 100.0\% | 95.65\% | 0.193 |
|  | TT004 | 81.81\% | 100.0\% | 90.00\% | 0.168 | 81.81\% | 100.0\% | 90.00\% | 0.096 | 81.81\% | 100.0\% | 90.00\% | 0.195 |
|  | TT005 | 92.85\% | 100.0\% | 96.29\% | 0.122 | 92.85\% | 100.0\% | 96.29\% | 0.100 | 86.66\% | 100.0\% | 92.28\% | 0.198 |
|  | TT006 | 90.00\% | 100.0\% | 94.73\% | 0.123 | 90.00\% | 100.0\% | 94.73\% | 0.116 | 90.00\% | 100.0\% | 94.73\% | 0.194 |
|  | TT010 | 81.81\% | 100.0\% | 90.00\% | 0.100 | 81.81\% | 100.0\% | 90.00\% | 0.098 | 81.81\% | 100.0\% | 90.00\% | 0.197 |
|  | TT013 | 85.71\% | 100.0\% | 92.30\% | 0.102 | 85.71\% | 100.0\% | 92.30\% | 0.097 | 85.71\% | 100.0\% | 92.30\% | 0.197 |
|  | TT014 | $85.71 \%$ | 100.0\% | 92.30\% | 0.100 | 85.71\% | 100.0\% | 92.30\% | 0.104 | 85.71\% | 100.0\% | 92.30\% | 0.201 |
|  | TT015 | 90.00\% | 90.00\% | 90.00\% | 0.101 | 90.90\% | 100.0\% | 95.23\% | 0.105 | 90.90\% | 100.0\% | 95.23\% | 0.197 |
|  | TT017 | 85.71\% | 100.0\% | 92.30\% | 0.100 | 85.71\% | 100.0\% | 92.30\% | 0.105 | 85.71\% | 100.0\% | 92.30\% | 0.211 |
|  | TT021 | 81.25\% | 100.0\% | 88.00\% | 0.122 | 81.25\% | 100.0\% | 89.65\% | 0.153 | 76.47\% | 100.0\% | 86.66\% | 0.197 |
|  | TT022 | 88.23\% | 100.0\% | 93.75\% | 0.103 | 88.23\% | 100.0\% | 93.75\% | 0.103 | 88.23\% | 100.0\% | 93.75\% | 0.107 |
|  | TT024 | 81.81\% | 100.0\% | 90.00\% | 0.099 | 81.81\% | 100.0\% | 90.00\% | 0.100 | 81.81\% | 100.0\% | 90.00\% | 0.195 |
|  | TT026 | 92.30\% | 100.0\% | 96.00\% | 0.139 | 92.30\% | 100.0\% | 96.00\% | 0.131 | 92.30\% | 100.0\% | 96.00\% | 0.197 |
|  | TT027 | 87.50\% | 93.33\% | 90.32\% | 0.100 | 87.50\% | 93.33\% | 90.32\% | 0.100 | 87.50\% | 93.33\% | 90.32\% | 0.265 |
|  |  | 86.88\% | 98.80\% | 92.26\% | 0.112 | 86.94\% | 99.52\% | 92.75\% | 0.107 | 86.16\% | 99.52\% | 92.25\% | 0.196 |
| OFF-SDTW | TT003 | 91.66\% | 100.0\% | 95.65\% | 1.030 | 91.66\% | 100.0\% | 95.65\% | 2.104 | 91.66\% | 100.0\% | 95.65\% | 4.119 |
|  | TT004 | 81.81\% | 100.0\% | 90.00\% | 0.589 | 81.81\% | 100.0\% | 90.00\% | 1.317 | 90.00\% | 100.0\% | 94.73\% | 2.461 |
|  | TT005 | 100.0\% | 92.37\% | 96.00\% | 0.904 | 92.30\% | 92.30\% | 92.30\% | 1.339 | 85.71\% | 92.30\% | 88.88\% | 3.018 |
|  | TT006 | 81.81\% | 100.0\% | 90.00\% | 0.325 | 63.63\% | 77.77\% | 70.00\% | 0.622 | 18.18\% | 22.22\% | 20.00\% | 1.853 |
|  | TT010 | 80.00\% | 88.88\% | 84.21\% | 0.474 | 72.72\% | 88.88\% | 80.00\% | 0.862 | 63.63\% | 77.77\% | 70.00\% | 1.644 |
|  | TT013 | 90.90\% | 83.33\% | 86.95\% | 0.426 | 83.33\% | 83.33\% | 83.33\% | 0.843 | 83.33\% | 83.33\% | 83.33\% | 1.705 |
|  | TT014 | 91.66\% | 91.66\% | 91.66\% | 1.652 | 76.92\% | 83.33\% | 80.00\% | 3.381 | 76.92\% | 83.33\% | 80.00\% | 7.124 |
|  | TT015 | 100.0\% | 90.00\% | 94.73\% | 0.491 | 100.0\% | 90.00\% | 94.73\% | 0.990 | 80.00\% | 80.00\% | 80.00\% | 2.193 |
|  | TT017 | 83.33\% | 93.33\% | 93.33\% | 0.789 | 83.33\% | 83.33\% | 83.33\% | 1.580 | 76.92\% | 83.33\% | 80.00\% | 3.422 |
|  | TT021 | 91.66\% | 84.61\% | 88.00\% | 0.977 | 91.66\% | 84.61\% | 88.00\% | 1.104 | 91.66\% | 84.61\% | 88.00\% | 2.231 |
|  | TT022 | 86.67\% | 86.67\% | 86.67\% | 0.719 | 86.67\% | 86.67\% | 86.67\% | 1.342 | 88.66\% | 88.66\% | 88.66\% | 2.731 |
|  | TT024 | 88.88\% | 88.88\% | 88.88\% | 0.641 | 88.88\% | 88.88\% | 88.88\% | 1.364 | 80.00\% | 88.88\% | 84.21\% | 2.824 |
|  | TT026 | 83.33\% | 83.33\% | 83.33\% | 0.694 | 84.61\% | 91.66\% | 88.00\% | 1.287 | 69.23\% | 75.00\% | 72.00\% | 2.823 |
|  | TT027 | 92.85\% | 86.66\% | 89.65\% | 0.856 | 86.66\% | 86.66\% | 86.66\% | 1.761 | 86.66\% | 86.66\% | 86.66\% | 3.611 |
|  |  | 88.89\% | 90.69\% | 89.93\% | 0.754 | 84.58\% | 88.38\% | 86.25\% | 1.421 | 77.32\% | 81.86\% | 79.43\% | 2.982 |
| ON-DTW | TT003 | 90.90\% | 90.90\% | 90.90\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT004 | 88.88\% | 88.88\% | 88.88\% | 0.001 | 100.0\% | 11.11\% | 20.00\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT005 | 92.28\% | 100.0\% | 96.29\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT006 | 88.88\% | 88.88\% | 88.88\% | 0.001 | 100.0\% | 11.11\% | 20.00\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT010 | 90.00\% | 100.0\% | 94.73\% | 0.001 | 75.00\% | 33.33\% | 46.15\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT013 | 100.0\% | 100.0\% | 100.0\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT014 | 91.66\% | 91.66\% | 91.66\% | 0.001 | 100.0\% | 66.67\% | 80.00\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT015 | 100.0\% | 100.0\% | 100.0\% | 0.001 | 100.0\% | 10.00\% | 18.18\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT017 | 90.00\% | 75.00\% | 81.81\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT021 | 100.0\% | 92.30\% | 96.00\% | 0.001 | 100.0\% | 30.76\% | 86.66\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT022 | 91.66\% | 86.67\% | 92.85\% | 0.001 | 91.66\% | 73.33\% | 81.48\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT024 | 87.50\% | 77.77\% | 82.23\% | 0.001 | 80.00\% | 44.44\% | 57.14\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT026 | 90.90\% | 83.33\% | 86.95\% | 0.001 | 66.66\% | 16.66\% | 26.66\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  | TT027 | 92.85\% | 86.67\% | 89.65\% | 0.001 | 90.90\% | 66.66\% | 76.69\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
|  |  | 92.53\% | 90.14\% | 91.48\% | 0.001 | 64.58\% | 26.00\% | 36.64\% | 0.001 | 00.00\% | 00.00\% | 00.00\% | 0.001 |
| ON-GCVS | TT003 | 91.66\% | 100.0\% | 95.65\% | 0.014 | 91.66\% | 100.0\% | 95.65\% | 0.130 | 78.57\% | 100.0\% | 88.00\% | 0.054 |
|  | TT004 | 90.00\% | 100.0\% | 94.73\% | 0.016 | 90.00\% | 100.0\% | 94.73\% | 0.263 | 81.81\% | 100.0\% | 90.00\% | 0.073 |
|  | TT005 | 86.66\% | 100.0\% | 92.85\% | 0.017 | 86.66\% | 100.0\% | 92.85\% | 0.107 | 86.66\% | 100.0\% | 92.85\% | 0.065 |
|  | TT006 | 90.00\% | 100.0\% | 94.73\% | 0.015 | 90.00\% | 100.0\% | 94.73\% | 0.163 | 81.81\% | 100.0\% | 90.00\% | 0.052 |
|  | TT010 | 90.00\% | 100.0\% | 94.73\% | 0.020 | 90.00\% | 100.0\% | 94.73\% | 0.107 | 69.23\% | 100.0\% | 81.81\% | 0.054 |
|  | TT013 | 92.30\% | 100.0\% | 96.00\% | 0.018 | 92.30\% | 100.0\% | 96.00\% | 0.107 | 80.00\% | 100.0\% | 88.88\% | 0.049 |
|  | TT014 | 85.71\% | 100.0\% | 92.30\% | 0.015 | 85.71\% | 100.0\% | 92.30\% | 0.109 | 85.71\% | 100.0\% | 92.30\% | 0.050 |
|  | TT015 | 90.90\% | 100.0\% | 95.23\% | 0.016 | 90.00\% | 90.00\% | 90.00\% | 0.108 | 83.33\% | 100.0\% | 90.90\% | 0.073 |
|  | TT017 | 92.30\% | 100.0\% | 96.00\% | 0.014 | 85.71\% | 100.0\% | 92.30\% | 0.108 | 75.00\% | 100.0\% | 85.71\% | 0.059 |
|  | TT021 | 92.85\% | 100.0\% | 96.29\% | 0.014 | 76.47\% | 100.0\% | 86.66\% | 0.146 | 68.41\% | 100.0\% | 81.25\% | 0.033 |
|  | TT022 | 93.75\% | 100.0\% | 96.77\% | 0.013 | 88.23\% | 100.0\% | 93.75\% | 0.107 | 78.94\% | 100.0\% | 88.23\% | 0.062 |
|  | TT024 | 90.00\% | 100.0\% | 94.73\% | 0.050 | 90.00\% | 100.0\% | 94.73\% | 0.107 | 75.00\% | 100.0\% | 85.71\% | 0.025 |
|  | TT026 | 92.30\% | 100.0\% | 96.00\% | 0.021 | 92.30\% | 100.0\% | 96.00\% | 0.108 | 85.71\% | 100.0\% | 92.30\% | 0.059 |
|  | TT027 | 93.75\% | 100.0\% | 96.77\% | 0.047 | 93.75\% | 100.0\% | 96.77\% | 0.128 | 83.33\% | 100.0\% | 90.90\% | 0.052 |
|  |  | 90.87\% | 100.0\% | 95.19\% | 0.020 | 88.77\% | 99.28\% | 93.65\% | 0.128 | 79.53\% | 100.0\% | 88.48\% | 0.054 |



Fig. 3: Gait events midstance $(\bullet)$, toe-off $(\bullet)$, and heel-strike $(\vee)$ detected using the GCVS algorithm for right foot gyroscope sensor data in the sagittal plane. The zero-velocity event intervals are represented by gray background.

